pre calculus chapter 1

pre calculus chapter 1 serves as a foundational introduction to the world of precalculus, bridging the gap between algebra and calculus. This chapter typically covers essential concepts such as functions, their properties, and various types of equations that will be crucial for understanding more complex mathematical ideas. In this article, we will explore key topics such as the definition of functions, the different types of functions, transformations, and the importance of graphs. Each of these elements plays a vital role in a student's mathematical toolkit. By the end of this article, readers will have a comprehensive understanding of what to expect in precalculus chapter 1, including its fundamental concepts and applications.

- Introduction to Functions
- Types of Functions
- Function Notation
- Transformations of Functions
- Graphs of Functions
- Applications of Functions
- Conclusion

Introduction to Functions

Functions are one of the most critical concepts introduced in precalculus chapter 1. A function is a relation that uniquely associates members of one set with members of another set. In simpler terms, for every input (or x-value), there is exactly one output (or y-value). This concept is foundational because it helps in understanding how different quantities interact with one another in mathematical contexts.

Functions can be represented in various forms, including equations, graphs, and tables. Understanding the definition of a function is essential for students as it lays the groundwork for more advanced topics in calculus. The notation used for functions is also important; it allows for concise communication of mathematical ideas. In this section, we will delve deeper into the definition and examples of functions that are typically covered in this chapter.

Defining Functions

A function can be formally defined as a set of ordered pairs (x, y) such that each x-value corresponds to exactly one y-value. Mathematically, this can be expressed as:

f: $X \rightarrow Y$, where X is the domain (set of all possible x-values) and Y is the range (set of all possible y-values).

For example, consider the function defined by f(x) = 2x + 3. For each value of x, there is a unique value of f(x). If x = 2, then f(2) = 2(2) + 3 = 7. This uniqueness is what differentiates functions from other relations.

Evaluating Functions

Evaluating functions involves substituting values into the function's expression to find the corresponding output. This process is crucial for understanding how functions behave. Students often practice evaluating functions with different inputs to gain a better grasp of the concept.

Types of Functions

In precalculus chapter 1, students are introduced to various types of functions, each with distinct characteristics and applications. Understanding these types is crucial for successfully navigating more complex mathematical concepts in later chapters.

Linear Functions

Linear functions are among the simplest types of functions. They can be expressed in the form f(x) = mx + b, where m represents the slope and b represents the y-intercept. The graph of a linear function is a straight line, and its slope indicates the rate of change. Linear functions are widely used in real-world applications, such as calculating costs and predicting trends.

Quadratic Functions

Quadratic functions are expressed in the standard form $f(x) = ax^2 + bx + c$. The graph of a quadratic function is a parabola, which can open upwards or downwards depending on the value of a. Quadratic functions often model situations involving area, projectile motion, and other phenomena that exhibit a squared relationship.

Polynomial Functions

Polynomial functions extend the concept of linear and quadratic functions. They can be expressed in the form $f(x) = a_n x^n + a_{n-1} x^{n-1} + \ldots + a_1 x + a_0$, where n is a non-negative integer. Polynomial functions can have multiple turning points and are used in various fields, including physics and engineering.

Function Notation

Understanding function notation is essential for working with functions in precalculus. Function notation provides a way to write functions in a concise format that clearly identifies the input and output. The common notation is f(x), where f represents the function and x is the input value.

Reading Function Notation

When reading function notation, it is important to recognize that f(x) does not imply multiplication. Instead, it indicates the output of the function f for a given input x. For example, if $f(x) = x^2$, then $f(3) = 3^2 = 9$.

Using Function Notation

Function notation allows for easy communication of mathematical concepts. For instance, if a student is asked to find the value of a function at a specific point, they can simply substitute the value into the function's expression and calculate the result. This clarity is critical for solving more complex problems involving multiple functions.

Transformations of Functions

Transformations of functions involve shifting, reflecting, stretching, or compressing the graph of the function. Understanding these transformations is crucial for analyzing how changes to the function's equation affect its graph.

Types of Transformations

- Translations: Shifting the graph horizontally or vertically.
- Reflections: Flipping the graph over a specific axis.
- Stretching and Compressing: Altering the width or height of the graph.

Each type of transformation can be described mathematically. For example, the function $f(x) = (x - h)^2 + k$ represents a translation of the parent function $f(x) = x^2$, moving it h units to the right and k units up.

Graphs of Functions

The graph of a function visually represents the relationship between the input and output values. Graphing functions is an essential skill introduced in precalculus chapter 1, and it allows students to visualize how functions behave over different intervals.

Plotting Points

To graph a function, students typically start by creating a table of values. They choose several x-values, calculate the corresponding y-values using the function's equation, and then plot these points on a coordinate plane. Connecting these points provides a visual representation of the function.

Analyzing Graphs

Once a graph is created, students learn to analyze its features, such as intercepts, asymptotes, and intervals of increase or decrease. Understanding these characteristics is crucial for solving real-world problems and preparing for calculus concepts.

Applications of Functions

Functions have a wide range of applications in various fields, including science, engineering, economics, and everyday life. In precalculus chapter 1, students explore how functions can model real-world phenomena.

Real-World Examples

Functions can represent relationships such as:

- Distance and time in motion problems.
- Cost and quantity in economics.
- Population growth in biology.

By understanding how to apply functions to real-life scenarios, students can develop critical thinking and problem-solving skills that are invaluable in academic and professional settings.

Conclusion

Pre calculus chapter 1 serves as a vital introduction to the concepts and applications of functions. Students learn about the definition of functions, various types, and their notations, along with transformations and graphical representations. The knowledge acquired in this chapter lays the groundwork for future studies in mathematics, particularly calculus. As students progress through their studies, the skills they gain in understanding and manipulating functions will be crucial for tackling more advanced mathematical challenges.

Q: What is a function in mathematics?

A: A function is a relation that associates each input from a set (domain) with exactly one output from another set (range).

Q: What are the different types of functions introduced in precalculus chapter 1?

A: The primary types of functions include linear functions, quadratic functions, and polynomial functions, each with distinct properties and applications.

Q: How do you evaluate a function?

A: Evaluating a function involves substituting a specific input value into the function's equation to determine the corresponding output.

Q: What does function notation mean?

A: Function notation, such as f(x), indicates the output of a function for a given input x, allowing for clear communication of mathematical ideas.

Q: Why are transformations of functions important?

A: Transformations allow students to understand how changes to a function's equation affect its graph, which is essential for graphing and analyzing functions.

Q: How do you graph a function?

A: To graph a function, you can create a table of values by choosing x-values, calculating corresponding y-values, and then plotting these points on a coordinate plane.

Q: What are some real-world applications of functions?

A: Functions can model various relationships, such as distance and time in motion problems, cost and quantity in economics, and population growth in biology.

Q: What is the importance of understanding functions in precalculus?

A: Understanding functions is crucial as they form the basis for more advanced topics in calculus and are applicable in various real-world situations across multiple fields.

Pre Calculus Chapter 1

Find other PDF articles:

 $\underline{https://explore.gcts.edu/gacor1-29/Book?trackid=VvZ26-6854\&title=wolfers-economics-textbook-principles.pdf}$

pre calculus chapter 1: Pre-Calculus For Dummies Krystle Rose Forseth, Christopher Burger, Michelle Rose Gilman, Deborah J. Rumsey, 2008-04-07 Offers an introduction to the principles of pre-calculus, covering such topics as functions, law of sines and cosines, identities, sequences, series, and binomials.

pre calculus chapter 1: *Pre-Calculus For Dummies* Mary Jane Sterling, 2018-11-13 Get ahead in pre-calculus Pre-calculus courses have become increasingly popular with 35 percent of students in the U.S. taking the course in middle or high school. Often, completion of such a course is a prerequisite for calculus and other upper level mathematics courses. Pre-Calculus For Dummies is an invaluable resource for students enrolled in pre-calculus courses. By presenting the essential topics in a clear and concise manner, the book helps students improve their understanding of pre-calculus and become prepared for upper level math courses. Provides fundamental information in an approachable manner Includes fresh example problems Practical explanations mirror today's teaching methods Offers relevant cultural references Whether used as a classroom aid or as a refresher in preparation for an introductory calculus course, this book is one you'll want to have on hand to perform your very best.

pre calculus chapter 1: Pre-Calculus All-in-One For Dummies Mary Jane Sterling, 2023-10-10 The easy way to understand and retain all the concepts taught in pre-calculus classes Pre-Calculus All-in-One For Dummies is a great resource if you want to do you best in Pre-Calculus. Packed with lessons, examples, and practice problems in the book, plus extra chapter quizzes online, it gives you absolutely everything you need to succeed in pre-calc. Unlike your textbook, this book presents the essential topics clearly and concisely, so you can really understand the stuff you learn in class, score high on your tests (including the AP Pre-Calculus exam!), and get ready to confidently move ahead to upper-level math courses. And if you need a refresher before launching into calculus, look no further—this book has your back. Review what you learned in algebra and geometry, then dig into pre-calculus Master logarithms, exponentials, conic sections, linear equations, and beyond Get easy-to-understand explanations that match the methods your teacher uses Learn clever shortcuts, test-taking tips, and other hacks to make your life easier Pre-Calculus All-in-One For Dummies is the must-have resource for students who need to review for exams or just want a little (or a lot of!) extra help understanding what's happening in class.

pre calculus chapter 1: Pre-Calculus Workbook For Dummies Mary Jane Sterling, 2019-04-02 Get a handle on pre-calculus in a pinch! If you're tackling pre-calculus and want to up your chances of doing your very best, this hands-on workbook is just what you need to grasp and retain the concepts that will help you succeed. Inside, you'll get basic content review for every concept, paired with examples and plenty of practice problems, ample workspace, step-by-step solutions, and thorough explanations for each and every problem. In Pre-Calculus Workbook For Dummies, you'll also get free access to a quiz for every chapter online! With all of the lessons and practice offered, you'll memorize the most frequently used formulas, see how to avoid common mistakes, understand tricky trig proofs, and get the inside scoop on key concepts such as quadratic equations. Get ample review before jumping into a calculus course Supplement your classroom work with easy-to-follow guidance Make complex formulas and concepts more approachable Be prepared to further your mathematics studies Whether you're enrolled in a pre-calculus class or you're looking for a refresher as you prepare for a calculus course, this is the perfect study companion to make it easier.

pre calculus chapter 1: Pre-Calculus For Dummies Yang Kuang, Elleyne Kase, 2012-06-26 Offers an introduction to the principles of pre-calculus, covering such topics as functions, law of sines and cosines, identities, sequences, series, and binomials.

pre calculus chapter 1: *Pre-Calculus, Calculus, and Beyond* Hung-Hsi Wu, 2020-10-26 This is the last of three volumes that, together, give an exposition of the mathematics of grades 9-12 that is simultaneously mathematically correct and grade-level appropriate. The volumes are consistent with CCSSM (Common Core State Standards for Mathematics) and aim at presenting the mathematics of K-12 as a totally transparent subject. This volume distinguishes itself from others of the same genre in getting the mathematics right. In trigonometry, this volume makes explicit the fact that the trigonometric functions cannot even be defined without the theory of similar triangles. It also provides details for extending the domain of definition of sine and cosine to all real numbers. It explains as well why radians should be used for angle measurements and gives a proof of the conversion formulas between degrees and radians. In calculus, this volume pares the technicalities

concerning limits down to the essential minimum to make the proofs of basic facts about differentiation and integration both correct and accessible to school teachers and educators; the exposition may also benefit beginning math majors who are learning to write proofs. An added bonus is a correct proof that one can get a repeating decimal equal to a given fraction by the "long division" of the numerator by the denominator. This proof attends to all three things all at once: what an infinite decimal is, why it is equal to the fraction, and how long division enters the picture. This book should be useful for current and future teachers of K-12 mathematics, as well as for some high school students and for education professionals.

pre calculus chapter 1: *Pre-Calculus Workbook For Dummies?* Michelle Rose Gilman, Christopher Burger, Karina Neal, 2009-06-24 Get the confidence and the math skills you need to get started with calculus! Are you preparing for calculus? This easy-to-follow, hands-on workbook helps you master basic pre-calculus concepts and practice the types of problems you'll encounter in your cour sework. You get valuable exercises, problem-solving shortcuts, plenty of workspace, and step-by-step solutions to every problem. You'll also memorize the most frequently used equations, see how to avoid common mistakes, understand tricky trig proofs, and much more. 100s of Problems! Detailed, fully worked-out solutions to problems The inside scoop on quadratic equations, graphing functions, polynomials, and more A wealth of tips and tricks for solving basic calculus problems

pre calculus chapter 1: Pre-Calculus Workbook For Dummies Yang Kuang, Michelle Rose Gilman, 2011-03-16 Get the confidence and math skills you need to get started with calculus Are you preparing for calculus? This hands-on workbook helps you master basic pre-calculus concepts and practice the types of problems you'll encounter in the course. You'll get hundreds of valuable exercises, problem-solving shortcuts, plenty of workspace, and step-by-step solutions to every problem. You'll also memorize the most frequently used equations, see how to avoid common mistakes, understand tricky trig proofs, and much more. Pre-Calculus Workbook For Dummies is the perfect tool for anyone who wants or needs more review before jumping into a calculus class. You'll get guidance and practical exercises designed to help you acquire the skills needed to excel in pre-calculus and conquer the next contender-calculus. Serves as a course guide to help you master pre-calculus concepts Covers the inside scoop on quadratic equations, graphing functions, polynomials, and more Covers the types of problems you'll encounter in your coursework With the help of Pre-Calculus Workbook For Dummies you'll learn how to solve a range of mathematical problems as well as sharpen your skills and improve your performance.

pre calculus chapter 1: *Precalculus* Mustafa A. Munem, James P. Yizze, 2002-10-07 pre calculus chapter 1: *Precalculus* Cynthia Y. Young, 2010-01-19 Engineers looking for an accessible approach to calculus will appreciate Young's introduction. The book offers a clear writing style that helps reduce any math anxiety they may have while developing their problem-solving skills. It incorporates Parallel Words and Math boxes that provide detailed annotations which follow a multi-modal approach. Your Turn exercises reinforce concepts by allowing them to see the connection between the exercises and examples. A five-step problem solving method is also used to help engineers gain a stronger understanding of word problems.

pre calculus chapter 1: *Linear Algebra* Tom M. Apostol, 2014-08-22 Developed from the author's successful two-volume Calculus text this book presents Linear Algebra without emphasis on abstraction or formalization. To accommodate a variety of backgrounds, the text begins with a review of prerequisites divided into precalculus and calculus prerequisites. It continues to cover vector algebra, analytic geometry, linear spaces, determinants, linear differential equations and more

pre calculus chapter 1: Precalculus with Trigonometry Paul A. Foerster, 2003 Precalculus with Trigonometry: Concepts and Applications

pre calculus chapter 1: *Pre-Calculus Essentials* Ernest Woodward, 2013-01-01 REA's Essentials provide quick and easy access to critical information in a variety of different fields, ranging from the most basic to the most advanced. As its name implies, these concise,

comprehensive study guides summarize the essentials of the field covered. Essentials are helpful when preparing for exams, doing homework and will remain a lasting reference source for students, teachers, and professionals. Pre-Calculus reviews sets, numbers, operations and properties, coordinate geometry, fundamental algebraic topics, solving equations and inequalities, functions, trigonometry, exponents and logarithms, conic sections, matrices and determinants.

pre calculus chapter 1: Algebra and Geometry Hung-Hsi Wu, Hongxi Wu, 2020-09-08 This is the second of three volumes that, together, give an exposition of the mathematics of grades 9-12 that is simultaneously mathematically correct and grade-level appropriate. The volumes are consistent with CCSSM (Common Core State Standards for Mathematics) and aim at presenting the mathematics of K-12 as a totally transparent subject. The first part of this volume is devoted to the study of standard algebra topics: quadratic functions, graphs of equations of degree 2 in two variables, polynomials, exponentials and logarithms, complex numbers and the fundamental theorem of algebra, and the binomial theorem. Having translations and the concept of similarity at our disposal enables us to clarify the study of quadratic functions by concentrating on their graphs, the same way the study of linear functions is greatly clarified by knowing that their graphs are lines. We also introduce the concept of formal algebra in the study of polynomials with complex coefficients. The last three chapters in this volume complete the systematic exposition of high school geometry that is consistent with CCSSM. These chapters treat the geometry of the triangle and the circle, ruler and compass constructions, and a general discussion of axiomatic systems, including non-Euclidean geometry and the celebrated work of Hilbert on the foundations. This book should be useful for current and future teachers of K-12 mathematics, as well as for some high school students and for education professionals.

pre calculus chapter 1: Precalculus with Calculus Previews Dennis G. Zill, Jacqueline M. Dewar, 2015-11-03 Building off the success of Zill and Dewar's popular Essentials version, the new Sixth Edition of Precalculus with Calculus Previews continues to include all of the outstanding features and learning tools found in the original text while incorporating additional topics of coverage that some courses may require. With a continued effort to keep the text complete, yet concise, the authors have included four additional chapters making the text a clear choice for many mainstream courses. Additional chapters include a new chapter on Polar Coordinates, as well as Triangle Trigonometry, Systems of Equations and Inequalities, and Sequences and Series.

pre calculus chapter 1: Calculus Workbook For Dummies with Online Practice Mark Ryan, 2018-04-12 The easy way to conquer calculus Calculus is hard—no doubt about it—and students often need help understanding or retaining the key concepts covered in class. Calculus Workbook For Dummies serves up the concept review and practice problems with an easy-to-follow, practical approach. Plus, you'll get free access to a quiz for every chapter online. With a wide variety of problems on everything covered in calculus class, you'll find multiple examples of limits, vectors, continuity, differentiation, integration, curve-sketching, conic sections, natural logarithms, and infinite series. Plus, you'll get hundreds of practice opportunities with detailed solutions that will help you master the math that is critical for scoring your highest in calculus. Review key concepts Take hundreds of practice problems Get access to free chapter quizzes online Use as a classroom supplement or with a tutor Get ready to quickly and easily increase your confidence and improve your skills in calculus.

pre calculus chapter 1: Rational Numbers to Linear Equations Hung-Hsi Wu, 2020-06-18 This is the first of three volumes that, together, give an exposition of the mathematics of grades 9-12 that is simultaneously mathematically correct and grade-level appropriate. The volumes are consistent with CCSSM (Common Core State Standards for Mathematics) and aim at presenting the mathematics of K-12 as a totally transparent subject. The present volume begins with fractions, then rational numbers, then introductory geometry that can make sense of the slope of a line, then an explanation of the correct use of symbols that makes sense of "variables", and finally a systematic treatment of linear equations that explains why the graph of a linear equation in two variables is a straight line and why the usual solution method for simultaneous linear equations "by substitutions"

is correct. This book should be useful for current and future teachers of K-12 mathematics, as well as for some high school students and for education professionals.

pre calculus chapter 1: Calculus Workbook For Dummies Mark Ryan, 2005-08-05 From differentiation to integration - solve problems with ease Got a grasp on the terms and concepts you need to know, but get lost halfway through a problem or, worse yet, not know where to begin? Have no fear! This hands-on guide focuses on helping you solve the many types of calculus problems you encounter in a focused, step-by-step manner. With just enough refresher explanations before each set of problems, you'll sharpen your skills and improve your performance. You'll see how to work with limits, continuity, curve-sketching, natural logarithms, derivatives, integrals, infinite series, and more! 100s of Problems! Step-by-step answer sets clearly identify where you went wrong (or right) with a problem The inside scoop on calculus shortcuts and strategies Know where to begin and how to solve the most common problems Use calculus in practical applications with confidence

pre calculus chapter 1: Resources for the Study of Real Analysis Robert L. Brabenec, 2004 A collection of materials gathered by the author while teaching real analysis over a period of years.

pre calculus chapter 1: Schaum's Outline of PreCalculus, 2nd Ed. Fred Safier, 2008-08-31 Schaum's has Satisfied Students for 50 Years. Now Schaum's Biggest Sellers are in New Editions! For half a century, more than 40 million students have trusted Schaum's to help them study faster, learn better, and get top grades. Now Schaum's celebrates its 50th birthday with a brand-new look, a new format with hundreds of practice problems, and completely updated information to conform to the latest developments in every field of study. Schaum's Outlines-Problem Solved More than 100,000 sold! This book has been updated to reflect the latest course scope and sequence. Review problems have been added after key chapters as well as more supplementary practice problems. An informal level discussion of limits, continuity, and derivatives has also been added, as well as additional information on the algebra of the dot product, exponential form of complex numbers, and conic sections in polar coordinates-plus business applications such as average rate of change, price/demand and science applications, including projectiles.

Related to pre calculus chapter 1

-
000 pre 00000 - 00 000000000000000000000000000
$\mathbf{html} \ \square \ \mathbf{pre} \ \square \square \square \square - \square \square \ \mathbf{pre} \square \square$
[]+sid[]sit[][][][]"+ent[][=[][][][][][][][][][][][][][][][][][
$ \ \ presentation \ \ \ pre \ $
presentation [][] pre[][][][][][][][][][][][][][][][][][][]
Pre-A, AABCABC
LM-studio 2060
Physical Review E DDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDD
pre
$\mathbf{html} \; @ \; \mathbf{pre} \; @ \; \mathbf{pre} \; @ \; \mathbf{pre} \; \mathbf{mtml} \; < \mathbf{pre} \; \mathbf{mtml} \; \mathbf{pre} \; p$

```
0+sid_sit_000000"0"+ent_0=00000=000 000000
00000000 Pre-A000000A00 - 00 000000pre A00000000pre-A000000A00 00000preA00000
0+sid_sit_000000"0"+ent_0=00000=000 000000
 \  \, | \  \, presentation \  \, | \  \, | \  \, pre \  \, | \  \, | \  \, | \  \, pre \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \,
```

Physical Review E	Physical Review E 0000000000 PRE00000000000000000000000
000000000000000000000000000000000000000	

Back to Home: $\underline{\text{https://explore.gcts.edu}}$